ACMS Applied Math Seminar

Yang Yang Michigan Technological University Wednesday, January 31, 2024 154 Hurley Hall 3:30 PM – 4:30 PM

A Reinterpreted Discrete Fracture Model for Darcy-Forchheimer Flow in Fractured Porous Media

We propose a novel hybrid-dimensional model for the Darcy-Forchheimer flow in fractured rigid porous media, with a natural applicability to non-conforming meshes. Motivated by the previous work on the reinterpreted discrete fracture model (RDFM) for Darcy flows, we extend its key idea to non-Darcy flows. Coupling the Darcy's law in the matrix and the Forchheimer's law in the fractures through the introduction of the Dirac-functions to characterize the fractures, we derive a relationship between the total flow velocity in the porous media and the fluid velocity in the fractures. With this relation, it is natural to model the Darcy-Forchheimer flow in the whole computational domain by one equation. The local discontinuous Galerkin (LDG) method is applied for numerical discretization of the steady-state single-phase flow problem and a timemarching method is adopted to find the solution of the resulting nonlinear system. Besides, we construct a direct solver for the nonlinear equation of the fluid velocity in fracture to save computational cost. As an application, we discuss a simple transport model coupled with the flow equation. Several numerical experiments validate the performance of the model with its effectiveness on non-conforming meshes. We observe that the Darcy-Forchheimer model effectively reduces the flow rates and makes the predictions more realistic in case of excessive fracture velocities.

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